## Math 121 Take-Home Quiz #3 Due Sunday, February 18, 2024 in Gradescope by 11:59 pm ET

## Instructions:

- This is an Open Notes Quiz. You can use materials, homeworks problems, lecture notes, etc. that you manually worked on.
- This is **NOT** an Open Internet Quiz. You can only access our Main Course Webpage.
- You are not allowed to work on or discuss these problems with other students or people.
- You can ask a few small, clarifying, questions in Office Hours, but the problems will not be solved for you.
- The main goal is to make a thoughtful and detailed presentation for the solutions. Submit a clear final draft. No mess please.
- Please submit your final work in Gradescope in the Quiz 3 entry.

**1.** [10 Points] Show that 
$$\lim_{x\to 0} \frac{\ln(1-5x) + \arcsin(5x)}{3xe^x - \arctan(3x)} = \boxed{-\frac{25}{6}}$$

**2.** [10 Points] Show that 
$$\lim_{x \to \infty} \left(1 - \frac{8}{x^3}\right)^{x^3} = \boxed{e^{-8}}$$

**3.** [10 Points] Show that 
$$\lim_{x\to 0^+} x^3 \ln x = \boxed{0}$$

**4.** [10 Points] Show that 
$$\lim_{x \to \infty} \left( 1 - \arctan\left(\frac{3}{x^4}\right) \right)^{x^4} = e^{-3}$$

DO NOT SPEAK TO ANYONE ELSE ABOUT THIS QUIZ