

What you need to know for Exam 1

You should know Section 4.5, Sections 6.1–6.8, except Section 6.5. Also know Sections 7.1–7.3. The test will not explicitly cover material from earlier sections (or from Appendix D), but of course it will be assumed that you know what limits, derivatives, and integrals are, that you know how to use differentiation rules, and that you know some trigonometry. The following is a list of most of the topics covered. **THIS IS NOT A COMPREHENSIVE LIST, BUT MERELY AN AID.** Remember, no calculators in any exams.

- 4.5: The Substitution Rule, for both indefinite and definite integrals.
- 6.1: Know what one-to-one means and what an inverse function is. Know how the domain and range of f relate to the domain and range of f^{-1} .
- 6.2: Know the algebraic properties and limit properties of exponentials. The graph, derivative, and antiderivative of e^x . The chain rule with $e^{u(x)}$.
- 6.3: Algebraic properties of logarithms. The notion of $\ln(x)$ as the inverse function of e^x . The fact that $\ln e = 1$ and $\ln 1 = 0$. The graph and the limit properties of $\ln(x)$.
- 6.4: Derivative of $\ln(x)$ and antiderivative of $1/x$. The chain rule with $\ln(u(x))$. Know that $a^b = e^{b \ln a}$. See the Review Handout on e^x and $\ln x$.
- 6.6: The definition of inverse sine and tangent (not cosine or secant). The limit properties and the derivatives of $\arcsin x$ and $\arctan x$. Know the corresponding antiderivative formulas.
- 6.7: The definition of $\sinh x$ and $\cosh x$, and the identity $\cosh^2 x - \sinh^2 x = 1$. The graphs and derivatives of $\cosh x$ and $\sinh x$. Know what $\sinh 0$ and $\cosh 0$ equal.
- 6.8: L'Hôpital's Rule. Know the key hypothesis (that the original limit is one of the indeterminate forms $0/0$ or ∞/∞). Know how to apply it. Know how to use it to attack other indeterminate limits, like $0 \cdot \infty$, $\infty - \infty$, 0^0 , ∞^0 , and 1^∞ . Know NOT to apply it to NON-indeterminate forms (like $\infty/0$, $\infty \cdot \infty$, ∞^∞ , 0^∞ , and so on).
- Appendix D: This is just standard trig, so we didn't cover it in class, but you of course need to know all the fundamentals here. Know your trig values at standard angles.
- 7.1: Know the Integration by Parts rule, both for indefinite and for definite integrals. The LIPET mnemonic may help in choosing your u . Be able to apply Parts two or more times in a row, including things like the special trick of cycling through twice with say $\int e^x \sin x \, dx$.
- 7.2: Trig Integrals. Know how to integrate products of sines and cosines, like $\sin^5 x \cos^4 x$. See the book for a summary. Also know how to integrate simpler products of tangents and secants. Know the relevant trig identities for each case. What are the half-angle identities?
- 7.3: Trig substitution. Know what substitution to make given the forms shown in the box in the book. Triangle arguments (and trig identities, like $\sin(2x) = 2 \sin x \cos x$, if needed) to convert the final answer back to the original variable. Really practice here. Most of these integrals reduce at some point to integrals from previous sections.

Some things you don't need to know

- Section 4.5: The stuff about symmetry (page 334).
- Section 6.1: The *explicit* definitions of one-to-one and of inverse function. That is, you don't need to memorize those definitions. But you DO need to know the ideas of the definitions, including (but not limited to) stuff like the horizontal line test and the idea that the graph of f^{-1} is the mirror image of that of f across the line $y = x$.
- Section 6.2: Official definition of a^x for x irrational. The derivative of a^x for $a \neq e$. The official definition of the number e .
- Section 6.3: Logarithms to any base other than e .
- Section 6.4: Derivatives of logarithms to any base other than e . Logarithmic differentiation.
- All of Sections 6.2*, 6.3*, 6.4*.
- Section 6.6: The derivative or anything about \csc^{-1} and \cot^{-1} .
- Section 6.7: Hyperbolic functions other than $\sinh x$, $\cosh x$, or $\tanh x$. All the hyperbolic trig identities *besides* $\cosh^2 x - \sinh^2 x = 1$. Inverse hyperbolic functions. The formulas for inverse hyperbolic functions in terms of $\ln x$.
- Section 6.8: Cauchy's Mean Value Theorem and the proof of L'Hôpital's Rule.
- Section 7.2: Integrating $\tan^m x \sec^n x$ if m is even and n is odd. Also, integrating products of $\sin A$ and $\cos B$. (Sine and cosine of *different* things)
- Section 7.3: Completing the square (for now anyways).

Tips

- Do not drop limit signs. No! Don't do it...
- Study the Integration Reference Sheet carefully; know all of your basic integrals. No hesitation allowed! Know your trig. identities. Remember $+C$.
- Precisely learn each integration technique. Using these techniques, practice turning complicated integrals into the more basic ones on the Reference Sheet.
- Practice enough in order to *immediately* recognize which technique of integration is needed. There may be some flexibility here.
- For definite integrals, make sure that you change your limits of integration **every** time you make a substitution. They could be layered with multi-substitutions. in a single problem, so be careful. Otherwise, mark limits correctly. No mixing of variables.
- Know when ... and when **not** to apply L'H Rule.
- For L'Hôpital's rule, the main thing is to check that the limit in question looks like $0/0$ or ∞/∞ . So don't forget to check that. Then, be careful when differentiating. (Differentiate numerator and denominator **separately**; don't apply the quotient rule to the whole thing.)