Homework #21

Due Friday, May 13th in Gradescope by 11:59 pm ET

Goal: Exploring Polar Coordinates and their relation to Cartesian Coordinates, and Sketching Polar Curves.

For 1-3, Plot the point with the given Polar coordinates. Label everything. Then find the Cartesian coordinates of the point.

1.
$$(r,\theta) = \left(2, \frac{3\pi}{2}\right)$$
 2. $(r,\theta) = \left(\sqrt{2}, \frac{\pi}{4}\right)$ 3. $(r,\theta) = \left(-1, -\frac{\pi}{6}\right)$

$$2. (r, \theta) = \left(\sqrt{2}, \frac{\pi}{4}\right)$$

3.
$$(r,\theta) = \left(-1, -\frac{\pi}{6}\right)$$

For 4-5, Plot the point of the given Cartesian coordinates. Label everything.

First, find Polar coordinates (r, θ) of the point, where r > 0. Keep $0 \le \theta < 2\pi$.

Second, find Polar coordinates (r, θ) of the point, where r < 0. Keep $0 \le \theta < 2\pi$.

4.
$$(x,y) = (-4,4)$$

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 5. $(x,y) = (3,3\sqrt{3})$

For 6-9, Shade or Sketch the region in the plane consisting of points whose Polar coordinates satisfy the given conditions. Label everything.

6.
$$r \ge 1$$

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 7. $r \ge 0$ and $\frac{\pi}{4} \le \theta \le \frac{3\pi}{4}$

8.
$$1 \le r \le 3$$
 and $\frac{\pi}{6} < \theta < \frac{5\pi}{6}$ 9. $2 < r < 3$ and $\frac{4\pi}{3} \le \theta \le \frac{5\pi}{3}$

9.
$$2 < r < 3 \text{ and } \frac{4\pi}{3} \le \theta \le \frac{5\pi}{3}$$

For 10-14, Carefully sketch each of the following. Show all work. Also show both the Cartesian Plot and the final Polar plot. Label everything.

10.
$$r = 2\cos\theta$$
 11. $r = 3\sin\theta$

11
$$r - 3\sin\theta$$

12.
$$r = 1 + \sin \theta$$

13
$$r - 2 \pm 2 \cos \theta$$

12.
$$r = 1 + \sin \theta$$
 13. $r = 2 + 2\cos \theta$ 14. $r = 3 - 3\sin \theta$

IMPORTANT NOTE! You will be receiving an e-mail from the math department to fill out a course/teaching evaluation. These are important to me and the course and the College, so I will appreciate it if you take the time to fully fill them out. Thanks so much!

REGULAR OFFICE HOURS

Sunday: 6–7:30 pm TA Nico, SMUDD 207

Monday: 1:00–3:00 pm

6-7:30 pm TA Daksha, SMUDD 207

7:30–9:00 pm TA Karime, SMUDD 207

Tuesday: 12:00–4:00 pm

6-7:30 pm TA Ian, SMUDD 207

7:30–9:00 pm TA Nico, SMUDD 207

Wednesday: 1:00-3:00 pm

9–10:30 pm TA Daksha, SMUDD 207

Thursday: none for Professor

6–7:30 pm TA Ian, SMUDD 207

7:30-9:00 pm TA Karime, SMUDD 207

Friday: 12:00–2:00 pm

Keep reading your notes every night...