## Math 121 Take-Home Quiz #2

## Due Sunday, March 7, 2021 in Gradescope by 11:59 pm ET

## Instructions:

• This is an Open Notes Quiz. You can use materials, homeworks problems, lecture notes, etc. that you manually worked on.

- This is **NOT** an Open Internet Quiz. You can only access our Main Course Webpage.
- You are not allowed to work on or discuss these problems with other students or people.

• You can ask a few small, clarifying, questions in Office Hours, but the problems will not be solved for you.

• The main goal is to make a thoughtful and detailed presentation for the solutions. Submit a clear final draft. No mess please.

• Please submit your final work in Gradescope in the Quiz 2 entry.

**1.** [10 Points] Show that 
$$\lim_{x \to 0} \frac{\ln(1-5x) + \arcsin(5x)}{3xe^x - \arctan(3x)} = -\frac{25}{6}$$

**2.** [10 Points] Show that 
$$\lim_{x \to \infty} \left(1 - \frac{8}{x^3}\right)^{x^3} = \boxed{e^{-8}}$$

**3.** [10 Points] Show that 
$$\int_0^1 (x+1) \arctan x \, dx = \left\lfloor \frac{\pi - 1 - \ln 2}{2} \right\rfloor$$

Hint: You can work the integral right away OR you can distribute the  $\arctan x$  and split it up into two pieces.

## **Optional Bonus:** [+ 2 extra points] Compute $\int \ln(3x^2+4) dx$ .

This is an optional problem, and you only will get bonus points for a fully correct solution.