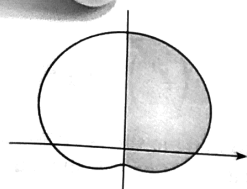
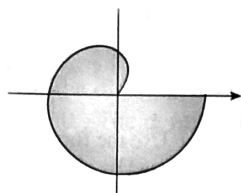


7.



$$r = 4 + 3 \sin \theta$$

8.



$$r = \sqrt{\ln \theta}, 1 \leq \theta \leq 2\pi$$

9–12 Sketch the curve and find the area that it encloses.

9.  $r = 2 \sin \theta$

10.  $r = 1 - \sin \theta$

11.  $r = 3 + 2 \cos \theta$

12.  $r = 2 - \cos \theta$

13–16 Graph the curve and find the area that it encloses.

13.  $r = 2 + \sin 4\theta$

14.  $r = 3 - 2 \cos 4\theta$

15.  $r = \sqrt{1 + \cos^2(5\theta)}$

16.  $r = 1 + 5 \sin 6\theta$

17–21 Find the area of the region enclosed by one loop of the curve.

17.  $r = 4 \cos 3\theta$

18.  $r^2 = 4 \cos 2\theta$

19.  $r = \sin 4\theta$

20.  $r = 2 \sin 5\theta$

21.  $r = 1 + 2 \sin \theta$  (inner loop)

22. Find the area enclosed by the loop of the strophoid  $r = 2 \cos \theta - \sec \theta$ .

23–28 Find the area of the region that lies inside the first curve and outside the second curve.

23.  $r = 4 \sin \theta, r = 2$

24.  $r = 1 - \sin \theta, r = 1$

25.  $r^2 = 8 \cos 2\theta, r = 2$

26.  $r = 1 + \cos \theta, r = 2 - \cos \theta$

27.  $r = 3 \cos \theta, r = 1 + \cos \theta$

28.  $r = 3 \sin \theta, r = 2 - \sin \theta$

29–34 Find the area of the region that lies inside both curves.

29.  $r = 3 \sin \theta, r = 3 \cos \theta$

30.  $r = 1 + \cos \theta, r = 1 - \cos \theta$

31.  $r = \sin 2\theta, r = \cos 2\theta$

32.  $r = 3 + 2 \cos \theta, r = 3 + 2 \sin \theta$

33.  $r^2 = 2 \sin 2\theta, r = 1$

34.  $r = a \sin \theta, r = b \cos \theta, a > 0, b > 0$

35. Find the area inside the larger loop and outside the smaller loop of the limaçon  $r = \frac{1}{2} + \cos \theta$ .

36. Find the area between a large loop and the enclosed small loop of the curve  $r = 1 + 2 \cos 3\theta$ .

37–42 Find all points of intersection of the given curves.

37.  $r = \sin \theta, r = 1 - \sin \theta$

38.  $r = 1 + \cos \theta, r = 1 - \sin \theta$

39.  $r = 2 \sin 2\theta, r = 1$

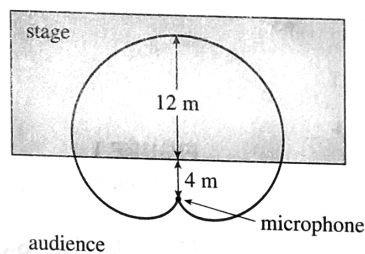
40.  $r = \cos 3\theta, r = \sin 3\theta$

41.  $r = \sin \theta, r = \sin 2\theta$

42.  $r^2 = \sin 2\theta, r^2 = \cos 2\theta$

43. The points of intersection of the cardioid  $r = 1 + \sin \theta$  and the spiral loop  $r = 2\theta, -\pi/2 \leq \theta \leq \pi/2$ , can't be found exactly. Use a graphing device to find the approximate values of  $\theta$  at which they intersect. Then use these values to estimate the area that lies inside both curves.

44. When recording live performances, sound engineers often use a microphone with a cardioid pickup pattern because it suppresses noise from the audience. Suppose the microphone is placed 4 m from the front of the stage (as in the figure) and the boundary of the optimal pickup region is given by the cardioid  $r = 8 + 8 \sin \theta$ , where  $r$  is measured in meters and the microphone is at the pole. The musicians want to know the area they will have on stage within the optimal pickup range of the microphone. Answer their question.



45–48 Find the exact length of the polar curve.

45.  $r = 2 \cos \theta, 0 \leq \theta \leq \pi$

46.  $r = 5^\theta, 0 \leq \theta \leq 2\pi$

47.  $r = \theta^2, 0 \leq \theta \leq 2\pi$

48.  $r = 2(1 + \cos \theta)$

49–50 Find the exact length of the curve. Use a graph to determine the parameter interval.

49.  $r = \cos^4(\theta/4)$

50.  $r = \cos^2(\theta/2)$