



FIGURE 19

Members of the family of limaçons $r = 1 + c \sin \theta$

The remaining parts of Figure 19 show that as c becomes negative, the shapes change in reverse order. In fact, these curves are reflections about the horizontal axis of the corresponding curves with positive c .

Limaçons arise in the study of planetary motion. In particular, the trajectory of Mars, as viewed from the planet Earth, has been modeled by a limaçon with a loop, as in the parts of Figure 19 with $|c| > 1$.

10.3 EXERCISES

1–2 Plot the point whose polar coordinates are given. Then find two other pairs of polar coordinates of this point, one with $r > 0$ and one with $r < 0$.

1. (a) $(1, \pi/4)$ (b) $(-2, 3\pi/2)$ (c) $(3, -\pi/3)$
 2. (a) $(2, 5\pi/6)$ (b) $(1, -2\pi/3)$ (c) $(-1, 5\pi/4)$

3–4 Plot the point whose polar coordinates are given. Then find the Cartesian coordinates of the point.

3. (a) $(2, 3\pi/2)$ (b) $(\sqrt{2}, \pi/4)$ (c) $(-1, -\pi/6)$
 4. (a) $(4, 4\pi/3)$ (b) $(-2, 3\pi/4)$ (c) $(-3, -\pi/3)$

5–6 The Cartesian coordinates of a point are given.

- (i) Find polar coordinates (r, θ) of the point, where $r > 0$ and $0 \leq \theta < 2\pi$.
 (ii) Find polar coordinates (r, θ) of the point, where $r < 0$ and $0 \leq \theta < 2\pi$.

5. (a) $(-4, 4)$ (b) $(3, 3\sqrt{3})$
 6. (a) $(\sqrt{3}, -1)$ (b) $(-6, 0)$

7–12 Sketch the region in the plane consisting of points whose polar coordinates satisfy the given conditions.

7. $r \geq 1$
 8. $0 \leq r < 2, \pi \leq \theta \leq 3\pi/2$
 9. $r \geq 0, \pi/4 \leq \theta \leq 3\pi/4$
 10. $1 \leq r \leq 3, \pi/6 < \theta < 5\pi/6$
 11. $2 < r < 3, 5\pi/3 \leq \theta \leq 7\pi/3$
 12. $r \geq 1, \pi \leq \theta \leq 2\pi$

13. Find the distance between the points with polar coordinates $(4, 4\pi/3)$ and $(6, 5\pi/3)$.

14. Find a formula for the distance between the points with polar coordinates (r_1, θ_1) and (r_2, θ_2) .

15–20 Identify the curve by finding a Cartesian equation for the curve.

15. $r^2 = 5$ 16. $r = 4 \sec \theta$
 17. $r = 5 \cos \theta$ 18. $\theta = \pi/3$
 19. $r^2 \cos 2\theta = 1$ 20. $r^2 \sin 2\theta = 1$