

- Please see the course webpage for the answer key.

Find the Interval and Radius of Convergence for the following Power Series. Analyze carefully and with full justification.

$$1. \sum_{n=0}^{\infty} \frac{(-1)^n (6x + 1)^n}{(6n + 1) 7^n}$$

$$2. \sum_{n=0}^{\infty} \frac{(-1)^n x^{2n+1}}{(2n + 1)!}$$

$$3. \sum_{n=0}^{\infty} n!(x - 9)^n$$

$$4. \sum_{n=0}^{\infty} \frac{(-1)^n (7x - 3)^n}{(n + 1) 5^n}$$

$$5. \sum_{n=0}^{\infty} n^n (3x + 5)^n$$

$$6. \sum_{n=0}^{\infty} \frac{x^n}{n!}$$

$$7. \sum_{n=0}^{\infty} \frac{(-1)^n (x + 5)^n}{(n + 3)^8 4^n}$$