• This is a closed-book examination. No books, notes, calculators, cell phones, communication devices of any sort, or other aids are permitted.

• Numerical answers such as $\sin\left(\frac{\pi}{6}\right)$, $4^{\frac{3}{2}}$, $\arctan(\sqrt{3})$, $e^{\ln 4}$, $\ln(e^7)$, or $e^{3\ln 3}$ should be simplified.

• Please *show* all of your work and *justify* all of your answers. (You may use the backs of pages for additional work space.)

1. Limits [30 Points total, 10 Points each] Evaluate each of the following. Please justify/simplify.

- (a) Show that $\lim_{x \to 0} \frac{\cos(3x) \arctan(2x) + 2x 1}{e^{-4x} 1 + 4x} = -\frac{9}{16}$
- (b) Show that $\lim_{x \to 0^+} \sqrt{x} \cdot \ln x = 0$
- (c) Show that $\lim_{x \to \infty} \left(1 \arcsin\left(\frac{2}{x^6}\right) \right)^{x^6} = \boxed{e^{-2}}$

Integrals [34 Points total] Compute each of the following Definite Integrals. Please justify/simplify.

- **2.** Show that $\int_{-2}^{2} \sqrt{4 x^2} \, dx = \boxed{2\pi}$
- **3.** Show that $\int_0^{\ln\sqrt{3}} \frac{e^x}{\sqrt{4 e^{2x}}} \, dx = \boxed{\frac{\pi}{6}}$
- **4.** Show that $\int_{e}^{e^3} \frac{1}{x [3 + (\ln x)^2]} dx = \boxed{\frac{\pi}{6\sqrt{3}}}$

More Integrals [36 Points total] Compute the following Indefinite Integrals. Please justify/simplify.

- **5.** Compute $\int x \arcsin x \, dx$
- 6. Compute $\int \frac{1}{(9+x^2)^{\frac{7}{2}}} dx$ Hint: $3^6 = 729$
- **7.** Compute $\int \ln (x^2 + 9) dx$