Math 121, Section(s) 01, 02, Fall 2023

Homework #17

Due Friday, November 17th in Gradescope by 11:59 pm ET

Goal: Exploring Estimating Values and Definite Integrals using the Alternating Series Estimation Theorem. Also some review of Interval and Radius of Convergence.

1. Use Series to Estimate $\frac{1}{e}$ with error less than $\frac{1}{20}$. Justify.

2. Use Series to Estimate $\frac{1}{e}$ with error less than $\frac{1}{100}$. Justify. (Can reuse work from 1)

3. Use Series to Estimate $\frac{1}{e}$ with error less than $\frac{1}{500}$. Justify. (Can reuse work from 1)

4. Use Series to Estimate sin(1) with error less than $\frac{1}{1000}$. Justify.

5. Use Series to Estimate $e^{-\frac{1}{3}}$ with error less than $\frac{1}{100}$. Justify.

- 6. Use Series to Estimate $\arctan\left(\frac{1}{2}\right)$ with error less than $\frac{1}{100}$. Justify.
- 7. Use Series to Estimate $\int_0^1 x \ln(1+x^3) dx$ with error less than $\frac{1}{20}$. Justify.

8. Use Series to Estimate
$$\int_0^1 x \sin(x^2) dx$$
 with error less than $\frac{1}{1000}$. Justify

Review: Find the Interval and Radius of Convergence for each of the following.

9.
$$\sum_{n=1}^{\infty} (n!)^2 (3x-7)^n$$
 10. $\sum_{n=1}^{\infty} \frac{(-1)^n (5x-2)^n}{n^3 8^n}$ 11. $\sum_{n=1}^{\infty} \frac{(x-7)^n}{n! \sqrt{n}}$

12. New! Use Series to compute $\lim_{x\to 0} \frac{1-\cos x}{1+x-e^x}$. Check answer with L'H Rule too.

REGULAR OFFICE HOURS

Monday: 12:00–3:00 pm

7:30–9:00 pm TA Admire, SMUDD 206

9:00–10:30 pm TA Aidee, SMUDD 206

Tuesday: 1:00–4:00 pm

6–7:30 pm TA Natalie, SMUDD 206

7:30–9:00 pm TA Gretta, SMUDD 206

9–10:30 pm TA Aidee, SMUDD 206

Wednesday: 1:00-3:00 pm

6–7:30 pm TA Admire, SMUDD 206

7:30–9:00 pm TA James, SMUDD 206

9–10:30 pm TA Natalie, SMUDD 206

Thursday: none for Professor

6:00–7:30 pm TA Gretta, SMUDD 206

7:30–9:00 pm TA James, SMUDD 206

Friday: 12:00-2:00 pm

Chase the fine details and make a full justification. YES! Vacation!