Math 121, Sections 01, 02, 03, Fall 2021

Homework #3

Due Wednesday, September 8th in Gradescope by 11:59 pm ET

Goal: Solidying Calculus for Inverse Sine and Inverse Tangent.

Differentiate the following functions. Simplify.

- 1. $f(x) = \tan^{-1}(x^2)$ 2. $f(x) = (\tan^{-1}(x))^2$ 3. $y = x \sin^{-1} x + \sqrt{1 - x^2}$ 4. $f(x) = \ln\left(1 - \arcsin\left(\frac{2}{x^4}\right)\right)$ 5. Find the value of the expression $\tan\left(\sin^{-1}\left(\frac{2}{3}\right)\right)$
- 6. Simplify the expression $\sin(\tan^{-1} x)$
- 7. Compute the Second Derivative for $f(x) = \arctan(2x)$
- 8. Compute the Second Derivative for $f(x) = \arcsin(6x)$
- 9. **Prove** that $\frac{d}{dx}\sin^{-1}(3x) = \frac{3}{\sqrt{1-9x^2}}$

10. **Prove** that
$$\frac{d}{dx} \tan^{-1}(5x) = \frac{5}{1+25x^2}$$

11. Use Integration to **Justify** that $\int \frac{1}{3+x^2} dx = \frac{1}{\sqrt{3}} \arctan\left(\frac{x}{\sqrt{3}}\right) + C$

Compute each of the following Integrals. Simplify.

$$12. \int \frac{x^2}{x^2 + 1} dx \qquad 13. \int \frac{x + 1}{x^2 + 1} dx \qquad 14. \int_{\frac{1}{\sqrt{3}}}^{\sqrt{3}} \frac{8}{1 + x^2} dx$$

$$15. \int_{0}^{\frac{1}{2}} \frac{\arcsin x}{\sqrt{1 - x^2}} dx \qquad 16. \int \frac{1}{\sqrt{1 - x^2} \cdot \sin^{-1} x} dx \qquad 17. \int_{1}^{3} \frac{1}{\sqrt{x(1 + x)}} dx$$

$$18. \int_{0}^{\ln 3} \frac{e^x}{1 + e^x} dx \qquad 19. \int_{0}^{\frac{1}{2}\ln 3} \frac{e^x}{1 + e^{2x}} dx \qquad 20. \int \frac{e^{2x}}{\sqrt{1 - e^{4x}}} dx$$

$$21. \int_{3}^{3\sqrt{3}} \frac{1}{\sqrt{36 - x^2}} + \frac{1}{9 + x^2} dx$$

REGULAR OFFICE HOURS

Monday: 1:00–3:00 pm

9–10:30 pm TA Mia, SMUDD 207

Tuesday: 12:00–4:00 pm

6–7:30 pm TA Ian, SMUDD 207

7:30–9:00 pm TA Karime, SMUDD 207

Wednesday: 1:00-3:00 pm

6–7:30 pm TA Ian, SMUDD 207

 $7{:}30{-}9{:}00~\mathrm{pm}$ TA Daksha, SMUDD 207

Thursday: none for Professor

1–2:30 pm TA Mia, SMUDD 207

7:30–9:00 pm TA Daksha, SMUDD 207

Friday: 12:00-2:00 pm

2:30–4:00 pm TA Karime, SMUDD 014**

• Please do not wait until the last night to start.

• Please stop by for help! Please try the homework before you come by though. Final Answer keys are posted on the webpage. Please do **not** look at them unless you have completed the problems. **They are not a replacement for my help or your understanding.**

• You can also find help at the Math Fellow (Mia, Ian, Karime or Daksha) sessions.