

6. [21 Points] Volumes of Revolution

(a) Consider the region bounded by $y = \arctan x$, $y = \frac{\pi}{4}$, and $x = 0$. Rotate this region about the horizontal line $y = -1$. Set-up, **BUT DO NOT EVALUATE!!**, the integral to compute the volume of the resulting solid using the Washer Method. Sketch the solid, along with one of the approximating washers.

(b) Consider the region bounded by $y = \ln x$, $y = 2$, and $x = 10$. Rotate this region about the vertical line $x = -1$. Set-up, **BUT DO NOT EVALUATE!!**, the integral to compute the volume of the resulting solid using the Cylindrical Shells Method. Sketch the solid, along with one of the approximating shells.

(c) Consider the region bounded by $y = 2 + e^x$, $y = \cos x$, $x = 0$ and $x = \frac{\pi}{2}$. Rotate this region about the vertical line $x = 5$. Set-up, **BUT DO NOT EVALUATE!!**, the integral to compute the volume of the resulting solid using the Cylindrical Shells Method. Sketch the solid, along with one of the approximating shells.

7. [12 Points] Parametric Equations

Consider the Parametric Curve given by $x = e^t + \frac{1}{1 + e^t}$ and $y = 2 \ln(1 + e^t)$.

COMPUTE the **Arclength** of this parametric curve for $0 \leq t \leq \ln 3$.

OPTIONAL BONUS

Do not attempt these unless you are completely done with the rest of the exam.

OPTIONAL BONUS #1

(a) Compute $\sum_{n=0}^{\infty} \frac{n^2 (\ln 3)^n}{n!}$

(b) Compute $1 - \frac{1}{e} - \frac{e^2}{2!} + \frac{1}{e^3 \cdot 3!} + \frac{e^4}{4!} - \frac{1}{e^5 \cdot 5!} - \frac{e^6}{6!} + \dots$

(c) Compute the MacLaurin Series for $f(x) = \frac{x}{(1 - 2x)^3}$ and state its Radius of Convergence.