- \bullet This is a closed-book examination. No books, notes, calculators, cell phones, communication devices of any sort, or other aids are permitted.
- Numerical answers such as $\sin\left(\frac{\pi}{6}\right)$, $4^{\frac{3}{2}}$, $\sinh(\ln 3)$, $e^{\ln 4}$, $\ln(e^7)$, or $e^{3\ln 3}$ should be simplified.
- ullet Please show all of your work and justify all of your answers. (You may use the backs of pages for additional work space.)
- 1. Limits [25 Points total] Evaluate each of the following. Please justify/simplify. Be clear if the limit equals a value, $+\infty$ or $-\infty$, or Does Not Exist.
- (a) Show that $\lim_{x\to 0} \frac{\ln(1-5x) + \arcsin(5x)}{3xe^x \arctan(3x)} = \boxed{-\frac{25}{6}}$
- (b) Show that $\lim_{x\to 0^+} x^5 \ln x = \boxed{0}$
- (c) Show that $\lim_{x \to \infty} \left(1 \arcsin\left(\frac{2}{x^4}\right) \right)^{x^4} = \boxed{e^{-2}}$

Integrals [75 Points total, 15 points each] Compute each of the following integrals. Please justify/simplify.

- **2.** Show that $\int_{e}^{e^3} \frac{1}{x \left[3 + (\ln x)^2 \right]} \ dx = \boxed{\frac{\pi}{6\sqrt{3}}}$
- **3.** Compute $\int \frac{1}{(4-x^2)^{\frac{3}{2}}} dx$
- **4.** Compute $\int x^2 \arcsin x \ dx$
- **5.** Show that $\int_{1}^{e^{2}} \sqrt{x} \cdot \ln x \ dx = \boxed{\frac{8e^{3} + 4}{9}}$
- **6.** Compute $\int \frac{1}{(x^2+4)^2} dx \stackrel{\text{hint}}{=} \int \frac{1}{(\sqrt{x^2+4})^4} dx$