

- This is a closed-book examination. No books, notes, calculators, cell phones, communication devices of any sort, or other aids are permitted.
- You need *not* simplify algebraically complicated answers. However, numerical answers such as $\sin\left(\frac{\pi}{6}\right)$, $4^{\frac{3}{2}}$, $\sinh(\ln 3)$, $e^{\ln 4}$, $\ln(e^7)$, or $e^{3\ln 3}$ should be simplified.
- Please *show* all of your work and *justify* all of your answers. (You may use the backs of pages for additional work space.)

1. [30 Points] Evaluate each of the following **limits**. Please justify your answers. Be clear if the limit equals a value, $+\infty$ or $-\infty$, or Does Not Exist.

(a) $\lim_{x \rightarrow 0} \frac{1 - \cosh(2x)}{x + \ln(1 - x)}$

(b) $\lim_{x \rightarrow 0} \frac{\arctan(3x)}{\arcsin(4x)}$

(c) $\lim_{x \rightarrow \infty} \left(e^{\frac{1}{x}} - \frac{4}{x} \right)^x$

2. [30 Points] Compute each of the following **definite integrals**. Please simplify your answers.

(a) $\int_0^{\ln 7} x \sinh x \, dx$

(b) $\int_1^{\sqrt{3}} \frac{x+1}{\sqrt{4-x^2}} \, dx$

(c) $\int_0^1 \left(x + \frac{1}{e^x} \right)^2 \, dx$

3. [40 Points] Compute each of the following **indefinite integrals**.

(a) $\int x \arcsin x \, dx$

(b) $\int \frac{1}{(x^2 + 4)^{\frac{5}{2}}} \, dx$

(c) $\int \ln(x^2 + 1) \, dx$

OPTIONAL BONUS

Do not attempt these unless you are completely done with the rest of the exam.

OPTIONAL BONUS #1 Compute the following **indefinite integral**.

1. $\int e^{\sqrt{1+\sqrt{x}}} \, dx$

OPTIONAL BONUS #2 Compute the following **indefinite integral**.

2. $\int \sec^3 x \, dx$