Math 121 Take-Home Quiz #5

Due Sunday, March 9, 2025 in Gradescope by 11:59 pm

Instructions:

• This is an Open Notes Quiz. You can use materials, homeworks problems, lecture notes, etc. that you manually worked on.

- This is **NOT** an Open Internet Quiz. You can only access our Main Course Webpage.
- You are not allowed to work on or discuss these problems with other students or people.

• You can ask a few small, clarifying, questions in Office Hours, but the problems will not be solved for you.

• The main goal is to make a thoughtful and detailed presentation for the solutions. Submit a clear final draft. No mess please.

• Please submit your final work in Gradescope in the Quiz 5 entry.

For problems 1 - 4, determine whether the given **Sequence** Converges or Diverges. If it converges, find the Limit. Justify. [5 points each]

$$1. \left\{ \frac{3n^5 - 6n^2 + 7}{8n^5 + 2n^4 - 1} \right\}_{n=1}^{\infty} \qquad 2. \left\{ \frac{n^7}{4\ln n} \right\}_{n=2}^{\infty} \qquad 3. \left\{ \frac{(2n-1)!}{(2n+1)!} \right\}_{n=1}^{\infty} \quad 4. \left\{ 2025 \right\}_{n=1}^{\infty}$$

- 5. [10 Points] Consider $\sum_{n=1}^{\infty} \frac{(-1)^n \ 3^{n+1}}{2^{3n-1}}$.
- First, explain why this **Series** Converges
- Second, show that the series Sum equals $-\frac{18}{11}$

For 6 and 7, determine whether the **Series** Converges or Diverges. Name any Convergence Test(s) you use, and justify all of your work. [10 points each]

6.
$$\sum_{n=2}^{\infty} \frac{n^7}{4 \ln n}$$
 (hint: your work from 2. above will help here...)

- 7. $\sum_{n=1}^{\infty} \frac{4}{n^7} + \frac{4^n}{7^n}$
- 8. [10 Points] Use **TWO different** Methods/Tests to show that $\sum_{n=1}^{\infty} 2025$ Diverges. Justify.

DO NOT SPEAK TO ANYONE ELSE ABOUT THIS QUIZ