

HOMEWORK #14 (Exam 2 Review Packet)

Due Wednesday March 26th in Gradescope by 11:59 pm ET

Limit Definition of the Definite Integral

1. Compute $\int_{-1}^3 2 - 3x^2 \, dx$ using two different methods:

- (a) Fundamental Theorem of Calculus and
- (b) Limit Definition.

Differentiation

2. Compute $g''(x)$ where $g(x) = \int_x^7 \sqrt{1 - \cos(2t)} \, dt$

Integration Evaluate each of the following integrals. Simplify if possible.

$$3. \int x^7 (30 - x^8)^6 \, dx$$

$$4. \int_{\pi}^{3\pi} \cos\left(\frac{x}{6}\right) \, dx$$

$$5. \int 7 \cos(5x) - 5 \sin(7x) \, dx$$

$$6. \int_0^{\frac{\pi}{2}} \frac{\sin x}{(7 + \cos x)^2} \, dx$$

$$7. \int_4^9 \frac{\sqrt{x} - x^2}{x} \, dx$$

$$8. \int_2^3 \frac{1}{x^2} \sin\left(\frac{\pi}{x}\right) \, dx$$

$$9. \int \frac{\sqrt{7}}{\sqrt{x}(\sqrt{x} + 4)^2} \, dx$$

$$10. \int_0^{\frac{\pi}{3}} \tan^3 x \cdot \sec^2 x \, dx$$

$$11. \int x \left(\sqrt{x^2 + 1} + \frac{1}{\sqrt{x^2 + 1}} \right) \, dx$$

$$12. \int x(x + 1)^{14} \, dx$$

Displacement–Total Distance

13. Suppose that the velocity of a moving particle is $v(t) = t^2 - 11t + 24$ feet per second.

- Sketch both $v(t)$ and $|v(t)|$ and the bounded area(s)
- Write the cases definition for $|v(t)|$.
- Set-up, but do NOT compute, the Definite Integrals that compute both the **Displacement** and **Total Distance** it travels between time $t = 0$ and $t = 8$ seconds.

REGULAR OFFICE HOURS

Monday: 12:00–3:00 pm

7:30–9:00 pm TA Andrew, SMUDD **207**

Tuesday: 1:00–4:00 pm

Wednesday: 1:00–3:00 pm

Thursday: none for Professor

8:00–9:30 pm TA Andrew, SMUDD **208A**

Friday: 12:00–2:00 pm

- Use this Homework to test your pacing for the Exam 2.
- Check the pacing, and aim to improve the response to the integration technique.