Math 106, Spring 2023

Homework #8

Due FRIDAY, March 3rd in Gradescope by 11:59 pm ET

Goal: Warm-Up Algebra for future Area Computations

For problems 1-6, i and n are some constants. Simplify, combine similar variables.

1. Consider f(x) = 6x + 5. Compute $f\left(\frac{4i}{n}\right)$ 2. Consider f(x) = 6x + 5. Compute $f\left(-2 + \frac{3i}{n}\right)$ 3. Consider $f(x) = x^2 - 6x - 7$. Compute $f\left(\frac{4i}{n}\right)$ 4. Consider $f(x) = x^2 - 6x - 7$. Compute $f\left(5 + \frac{2i}{n}\right)$ 5. Consider $f(x) = x^2 - 5x - 4$. Compute $f\left(\frac{3i}{n}\right)$ 6. Consider $f(x) = x^2 - 5x - 4$. Compute $f\left(-4 + \frac{5i}{n}\right)$

For problems 7-18, Evaluate each of the Limits. You may need to use algebra to decompose the Limit into simpler pieces. Also use *arrows* to show the size arguments, either growing large towards ∞ and/or small towards 0.

$$7. \lim_{n \to \infty} 8 \qquad 8. \lim_{n \to \infty} \frac{1}{n} \qquad 9. \lim_{n \to \infty} \frac{6}{n}$$

$$10. \lim_{n \to \infty} \frac{n+4}{n} \qquad 11. \lim_{n \to \infty} \frac{2n+1}{n} \qquad 12. \lim_{n \to \infty} \frac{n(n+4)}{n^2}$$

$$13. \lim_{n \to \infty} \frac{n(n+1)(4n+1)}{n^3} \qquad 14. \lim_{n \to \infty} \frac{6}{n^2} \left(\frac{n(n+1)}{2}\right)$$

$$15. \lim_{n \to \infty} \frac{9}{n^3} \left(\frac{n(n+1)(2n+1)}{6}\right) \qquad 16. \lim_{n \to \infty} \frac{15}{n^3} \left(\frac{n(n+1)(2n+1)}{6}\right)$$

$$17. \lim_{n \to \infty} \frac{36}{n^3} \left(\frac{n(n+1)(2n+1)}{6}\right) - \frac{100}{n^2} \left(\frac{n(n+1)}{2}\right) + \left(\frac{7}{n}\right) n$$

$$18. \lim_{n \to \infty} \frac{24}{n^3} \left(\frac{n(n+1)(2n+1)}{6}\right) - \frac{42}{n^2} \left(\frac{n(n+1)}{2}\right) + \left(\frac{5}{n}\right) n$$

REGULAR OFFICE HOURS

Monday: None this week

Tuesday: None this week

$7{:}30{-}9{:}000~\mathrm{pm}$ TA Ellerman, SMUDD 204

Wednesday: None this week

Thursday: TBA

7:30–9:00 pm TA Ellerman, SMUDD 207 Friday: 12:00–2:00 pm

- Present Final Drafts only please
- \bullet Justify all details, and show all steps