

Math 106 Exam 2 March 31, 2023



• This is a closed-book examination. No books, notes, calculators, cell phones, communication devices of any sort, webpages, or other aids are permitted.

• Simplify numerical answers such as $\sin\left(\frac{\pi}{6}\right)$ and $4^{\frac{3}{2}}$.

• Please *show* all of your work and *justify* all of your answers. (You may use the backs of pages for additional work space.)

1. [20 Points] Compute and show that $\int_{-1}^{2} 3 - 4x - x^2 dx = \boxed{0}$

using two different methods:

(a) Fundamental Theorem of Calculus

(b) Limit Definition of the Definite Integral.

2. [32 Points] Evaluate each of the following Indefinite Integrals. Simplify.

(a)
$$\int \frac{5}{\sqrt{x} \left(3 + \sqrt{x}\right)^7} dx$$

(b) $\int x^7 (9-x^8)^6 dx$

(c)
$$\int \frac{\sec^2 x}{\left(5 + \tan x\right)^3} \, dx$$

(d)
$$\int \frac{x}{(x-3)^9} \, dx$$

3. [32 Points] Evaluate each of the following Definite Integrals. Simplify.

(a) Show that
$$\int_{1}^{4} \frac{(x+1)(x-1)}{\sqrt{x}} dx = \boxed{\frac{52}{5}}$$

(b) Show that
$$\int_{\frac{\pi}{9}}^{\frac{\pi}{3}} \sin(3x) dx = \boxed{\frac{1}{2}}$$

(c) Show that
$$\int_{-\pi}^{3\pi} \cos\left(\frac{x}{2}\right) dx = \boxed{0}$$

(d) Show that
$$\int_{\frac{\pi}{6}}^{\frac{\pi}{3}} \frac{\sin x}{\cos^{3} x} dx = \boxed{\frac{4}{3}}$$

4. [8 Points] Compute the following Definite Integral. Show all details. Show that $\int_{-1}^{3} |x-2| + 1 = 9$

5. [8 Points] Compute
$$f(x)$$
 where $f'(x) = \frac{1}{x^3\sqrt{3 + \frac{6}{x^2}}}$ and $f(1) = -\frac{5}{2}$