

- This is a closed-book examination. No books, notes, calculators, cell phones, communication devices of any sort, or webpages, or other aids are permitted.

Derivatives Compute each of the following derivatives.

1. Show that $f''(x) = -\left(\frac{x^2 + 3x + \ln x + 1}{x^2(x + \ln x)^2}\right)$, where $f(x) = \ln(x + \ln x)$.
2. $g'(x)$, where $g(x) = e^x + \frac{1}{e^x} + x^e + \frac{1}{x^e} + \frac{x}{e} + \frac{e}{x} + ex + \frac{1}{ex} + e^{e^x+x} + e^{x-e} + (x-e)^e$.
Do not simplify.
3. $\frac{dy}{dx}$, if $ye^{x+y} + \sec^2 x = \ln(3x) + \sec y$.
4. y' where $y = x^{\sin x}$.
5. $\frac{d}{dx} \ln\left(\frac{e^{-\sin x} \sqrt{1 + \sec \sqrt{x}}}{(5 - x^7)^{-\frac{2}{3}}}\right)$
6. $f'(x)$ where $f(x) = \frac{e^{-x} \sin(e^x)}{e^x \cos(e^{-x})}$. Do not simplify.
7. $g'(x)$, where $g(x) = \sqrt{x} \ln x + \ln \sqrt{x} + \sqrt{x \ln x} + \frac{1}{x\sqrt{\ln x}}$. Do not simplify.

Integration Compute each of the following integrals:

8. $\int \frac{(x^{\frac{1}{3}} + 1)(1 - x^{\frac{2}{3}})}{x^2} dx$
9. $\int_{e^4}^{e^9} \frac{\sqrt{\ln x}}{3x} dx$
10. $\int_0^{\ln 2} \left(e^x + \frac{1}{e^{2x}}\right)^2 dx$
11. $\int e^x + \frac{1}{e^x} + x^e + \frac{1}{x^e} + \frac{x}{e} + \frac{e}{x} + ex + \frac{1}{ex} + e^{e^x+x} + e^{x-e} + (x-e)^e dx$ look familiar?
12. $\int_{\frac{\pi}{18}}^{\frac{\pi}{9}} \tan(3x) dx$

13. $\int \frac{1}{e^{3x}(1+e^{-3x})^{\frac{2}{9}}} dx$

14. $\int \frac{e^x}{(1+e^x)^2} dx$

15. $\int \frac{(1+e^x)^2}{e^x} dx$

16. $\int_0^1 \frac{x}{1+x^2} dx$

17. $\int e^{x^2+\ln x+1} dx$

Tangent Lines

18. Find the equation of the tangent line to the curve

$$f(x) = \frac{e^{3x}}{1+e^x} \text{ at the point where } x = \ln 2.$$

Curve Sketching

19. Let $f(x) = e^{-\frac{x^2}{2}}$.

For this function, discuss domain, vertical and horizontal asymptote(s), interval(s) of increase or decrease, local extreme value(s), concavity, and inflection point(s). Then use this information to present a detailed and labelled sketch of the curve.