

Due Sunday, February 16, 2025 in Gradescope by 11:59 pm

Instructions:

- This is an Open Notes Quiz. You can use materials, homeworks problems, lecture notes, etc. that you manually worked on.
- This is **NOT** an Open Internet Quiz. You can only access our Main Course Webpage.
- You are not allowed to work on or discuss these problems with other students, professor, Math Fellow TA or simply put anyone.
- You can ask a few small, clarifying, questions in Office Hours, but the problems will not be solved for you.
- The main goal is to make a thoughtful and detailed presentation for the solutions. Submit a clear final draft. No mess please.
- Please submit your final work in Gradescope in the Quiz 3 entry.

**1.** [30 points] Compute the **Most General Antiderivative** for each of the following.

$$(a) \int 4x^7 + \frac{7}{x^4} + x^{\frac{4}{7}} + \frac{1}{x^{\frac{7}{4}}} - \frac{4}{7x^{\frac{4}{7}}} - \frac{7}{4} + \frac{7}{4}x + \frac{1}{7x^7} - \frac{7}{4x^7} dx$$

$$(b) \int \frac{x^2}{2} + 3x^3 - \frac{x^4}{4} + \frac{2}{x^2} - \frac{1}{3x^3} + \frac{4}{x^4} dx$$

$$(c) \int \frac{\left(x^2 + \frac{1}{x}\right)\left(x + \frac{1}{x^2}\right)}{\sqrt{x}} dx$$

$$(d) \int \sec^2 x + 2 \sin x - \cos x - \frac{\sec x \tan x}{7} dx$$

$$(e) \int \left(\sqrt{x} + \frac{1}{\sqrt{x}}\right)(1+x) dx$$

**2.** [10 points] Consider a function  $f$  with  $f''(x) = -3 + 12x - 12x^2$  and that satisfies  $f'(1) = -4$  and  $f(0) = 4$ .

- (a) Find  $f(x)$ .                      (b) Use  $f(x)$  from (a) to Compute  $f(1)$ . Simplify.

**3.** [10 points] Consider a function  $f$  with  $f'(x) = \sec^2 x - 4 \sin x$  and that satisfies  $f(\pi) = -6$ .

- (a) Find  $f(x)$ .                      (b) Use  $f(x)$  from (a) to Compute  $f\left(\frac{\pi}{3}\right)$ . Simplify.

DO NOT SPEAK TO ANYONE ELSE ABOUT THIS QUIZ