#### Math 106, Spring 2024

### Homework #2

# Due Friday, February 2nd in Gradescope by 11:59 pm ET

## Review all Trigonometry Notes from class

Goal: Review More Derivatives, Trigonometry, Angles & Trigonometric Derivatives.

FIRST: Read through and understand the following Examples.

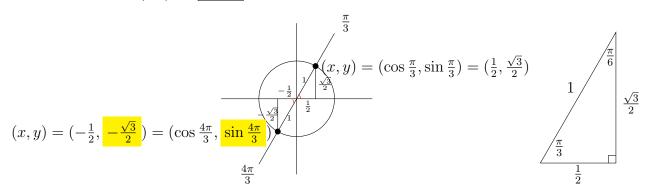
Ex: Differentiate 
$$f(x) = \frac{5}{(7x^3 - x^5)^6} \stackrel{\text{prep}}{=} 5 (7x^3 - x^5)^{-6}$$
.

Compute 
$$f'(x) = -30 (7x^3 - x^5)^{-7} (21x^2 - 5x^4)$$

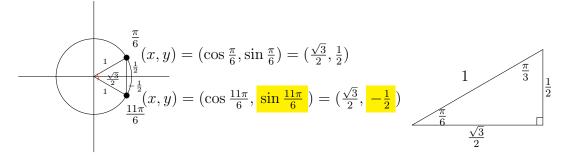
Ex: Differentiate 
$$G(x) = \left(\frac{1}{3x^7} - \frac{7}{x^3}\right)^4 \stackrel{\text{prep}}{=} \left(\frac{1}{3}x^{-7} - 7x^{-3}\right)^4$$
.

Compute 
$$f'(x) = 4\left(\frac{1}{3x^7} - \frac{7}{x^3}\right)^3 \cdot \left(-\frac{7}{3}x^{-8} + 21x^{-4}\right)$$

Ex: Show that  $\sin\left(\frac{4\pi}{3}\right) = \boxed{-\frac{\sqrt{3}}{2}}$ . Justify using the Unit Circle and the reference triangle.



Ex: Show that  $\sin\left(\frac{11\pi}{6}\right) = \boxed{-\frac{1}{2}}$ . Justify using the Unit Circle and the reference triangle.



Next, Complete the following Homework problems.

Match your final answers to the posted Answer Key.

For #1-5, compute the Derivative of each of the following functions. Do **Not** Simplify.

- 1.  $f(x) = \frac{4}{x^5} \frac{5}{4x} \frac{4}{5} + \frac{1}{4\sqrt{x}}$  2.  $y = (x^2 + 5x)^4$  3.  $y = \frac{1}{(x^2 + 5x)^4}$

- 4.  $y = \frac{1}{\sqrt{x^3 9x + 3}}$  5.  $y = \left(\frac{1}{r^3} + 7x\right)^{\frac{5}{7}} \left(x^4 \frac{1}{r^7}\right)^{-5}$

6. Compute the equation of the Tangent Line to  $y = 6\sqrt{2x+7}$  at the point where x = 1. Simplify.

7. Graph the function  $y = \sin x$  on the interval  $[0, 2\pi]$ . Determine the following values:

$$\sin 0 \quad \sin \frac{\pi}{2} \quad \sin \pi \quad \sin \frac{3\pi}{2} \quad \sin 2\pi$$

8. Graph the function  $f(x) = \cos x$  on the interval  $[0, 2\pi]$ . Determine the following values:

$$\cos 0 \quad \cos \frac{\pi}{2} \quad \cos \pi \quad \cos \frac{3\pi}{2} \quad \cos 2\pi$$

9. Make a chart of the Trig. Values for sine, cosine and tangent for all angles  $\theta = 0, \frac{\pi}{6}, \frac{\pi}{4}, \frac{\pi}{3}, \frac{\pi}{2}, \pi, \frac{3\pi}{2}, 2\pi$ 

For #10-15, compute the following values. Justify. Show work using Unit Circle and Trig Triangles.

- 10.  $\cos \frac{2\pi}{3}$  11.  $\sin \frac{5\pi}{3}$  12.  $\sin \frac{7\pi}{6}$  13.  $\cos \frac{5\pi}{4}$  14.  $\sin \frac{5\pi}{6}$

For #15-16, find the equation of the tangent line to f(x) at the given x-value. Simplify.

- 15.  $f(x) = \sin x$  at x = 0 16.  $f(x) = \cos x$  at  $x = \frac{\pi}{6}$

For #17 - 20, compute the Derivative for the following functions. Do **Not** Simplify.

- 17.  $y = \frac{1}{x} 2\cos x \sin x$  18.  $f(x) = \sqrt{x} \cdot \sin x$
- 19.  $f(x) = \cos x \cdot \sin x$  20.  $f(x) = \frac{\cos x}{x^2 + 3}$

# REGULAR OFFICE HOURS

Monday: 12:00–3:00 pm

Tuesday: 1:00–4:00 pm

Wednesday: 1:00-3:00 pm

Friday: 12:00-2:00 pm

Math Fellow evening TA Help Hours TBD soon

- Please take the time to read over your class notes this week.
- Work towards full understanding of the Trig concepts and not just the numbers and formulas.