## Math 106, Spring 2024

## Homework #13

Due Friday, March 15th in Gradescope by 11:59 pm ET

Goal: Computing Definite Integrals using the FTC and also u-substitution.

1. Compute  $\int_{-3}^{3} 3 - 4x - x^2 dx$  using Two different methods.

(a) Fundamental Theorem of Calculus

(b) Limit Definition of the Definite Integral.

Compute the following Indefinite Integrals. Simplify.

2. 
$$\int x^2 (1-x^3)^7 dx$$
 3.  $\int \frac{x^4}{(x^5-3)^8} dx$ 

$$3. \int \frac{x^4}{(x^5 - 3)^8} \ dx$$

4. 
$$\int \sec(3x)\tan(3x) \ dx$$

5. 
$$\int x^2 \cos(x^3 - 6) dx$$
 6. 
$$\int \frac{\sec^2\left(\frac{1}{x}\right)}{x^2} dx$$

$$6. \int \frac{\sec^2\left(\frac{1}{x}\right)}{x^2} dx$$

7. 
$$\int \cos^4 x \cdot \sin x \ dx$$

8. 
$$\int x\sqrt{4-x^2}\ dx$$

8. 
$$\int x\sqrt{4-x^2} \, dx$$
 9.  $\int \frac{x}{\sqrt{4-x^2}} \, dx$ 

10. 
$$\int \frac{\sin \sqrt{x}}{\sqrt{x}} dx$$

$$11. \int \frac{\cos x}{\sin^2 x} \ dx$$

11. 
$$\int \frac{\cos x}{\sin^2 x} dx$$
 12. 
$$\int \sqrt{x} \cdot \cos\left(9 + x^{\frac{3}{2}}\right) dx$$
 13. 
$$\int \frac{\cos x + \sin x}{(\cos x - \sin x)^3} dx$$

13. 
$$\int \frac{\cos x + \sin x}{(\cos x - \sin x)^3} dx$$

Compute the following Definite Integrals. Simplify. Remember to mark OR change your limits

14. 
$$\int_{\frac{\pi}{2}}^{\frac{\pi}{3}} \cos(4x) \ dx$$

14. 
$$\int_{\frac{\pi}{2}}^{\frac{\pi}{3}} \cos(4x) \ dx$$
 15.  $\int_{2\pi}^{6\pi} \sin\left(\frac{x}{6}\right) \ dx$  16.  $\int_{\frac{\pi}{4}}^{\frac{\pi}{3}} \frac{\sec^2 x}{\tan^3 x} \ dx$ 

16. 
$$\int_{\frac{\pi}{4}}^{\frac{\pi}{3}} \frac{\sec^2 x}{\tan^3 x} \, dx$$

17. If w'(t) is the rate of growth of a child in pounds per year, what does  $\int_{-\infty}^{\infty} w'(t) dt$  represent?

18. Consider velocity for a particle moving on a line given by v(t) = 3t - 6 meters per second.

• Compute both (a) the Displacement and (b) the Total Distance traveled by the particle when  $0 \le t \le 3$ .

• Sketch both v(t) and |v(t)|.

The second sketch |v(t)| will help you figure out the Absolute Value cases for the Total Distance formula.

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## REGULAR OFFICE HOURS

Monday: 12:00–3:00 pm

Tuesday: 1:00–4:00 pm

7:30–9:00 pm TA Alexa, SMUDD **208A** 

Wednesday: 1:00-3:00 pm

Thursday: none for Professor

6:00–7:30 pm TA Alexa, SMUDD **208A** 

Friday: 12:00-2:00 pm

- Check that you substitute all pieces. Check constants carefully.
- Definite Integral is a value. Indefinite Integral is a collection of functions.
  - Grab an extra hour a day to study. Happy Spring Break!