

Worksheet 1, Tuesday, September 10th, 2013

1. Simplify each of the following expressions. Show your work.

(a) $\frac{\left(\frac{a}{b}\right)}{\left(\frac{c}{d}\right)}$

(b) $\frac{1}{\left(\frac{a}{b}\right)}$

(c) $\frac{\left(\frac{a}{b}\right)}{c}$

(d) $\frac{a}{\left(\frac{b}{c}\right)}$

2. Solve each of the following equations (if possible):

(a) $x^2 - 4x - 21 = 0$

(b) $x^2 - x + 7 = 0$

(c) $x^2 + 2x - 4 = 0$

3. YES or NO: Does $\sqrt{x^2 + 4} = x + 2$? Why or why not?

4. Recall from class that we saw the graphs of $f(x) = \sqrt{x}$ and $g(x) = \frac{1}{x}$. Use these graphs to help you do the following:

(a) Sketch the graph of $F(x) = \sqrt{x+4}$. Discuss the Domain and Range for this new function.

(b) Sketch the graph of $G(x) = \frac{1}{x-6}$. Discuss the Domain and Range for this new function. Discuss the output behavior of $G(x)$ as the input value x is near $x = 6$. (Be specific.) Discuss the output behavior of $G(x)$ out near $\pm\infty$.

5. The Absolute Value Function $f(x) = |x|$ is a *piece-wise defined function* defined by

$$f(x) = |x| = \begin{cases} x & \text{if } x \geq 0 \\ -x & \text{if } x < 0 \end{cases}$$

(a) Give the Domain and Range for this function. Graph the absolute value function. Discuss how this function behaves near $x = 0$.

(b) Now consider $g(x) = |x - 6|$. Write out the piece-wise defined definition of this function carefully. THEN use that definition to graph the function g . Discuss how this graph relates to the graph of $f(x) = |x|$. Discuss how this function behaves near $x = 6$.

(c) Now consider $h(x) = |x + 7|$. Write out the piece-wise defined definition of this function carefully. THEN use that definition to graph the function h . Discuss how this graph relates to the graph of $f(x) = |x|$. Discuss how this function behaves near $x = -7$.

6. Find the equation of the line L that passes through the point $(3, -1)$ and is **perpendicular** to the line $2x + 5y = 6$. THEN, does this new line L pass through the point $(1, -6)$?
7. Consider the function $f(x) = x^2 - 6x - 7$. Compute and **simplify** each of the following.
- $f(0)$
 - $f(-3)$
 - $f(1)$
 - For what values x does $f(x) = 0$?
 - $f(a)$
 - $f(a + h)$
 - $\frac{f(a + h) - f(a)}{h}$
 - CHALLENGE!!!** Compute $f(f(x))$. Show that it equals $x^4 - 12x^3 + 16x^2 + 120x + 84$. Yes... simplify! Come on you can try it...
8. Consider the function defined piece-wise by

$$f(x) = \begin{cases} x + 2 & \text{if } x > 2 \\ -3 & \text{if } x = 2 \\ x^2 & \text{if } -1 < x < 2 \\ 5 & \text{if } x < -1 \end{cases}$$

Graph $f(x)$ and find its Domain and Range.

9. Consider the function defined piece-wise by

$$g(x) = \begin{cases} \frac{1}{x} & \text{if } x > 0 \\ -\frac{1}{2}x + 1 & \text{if } -4 < x \leq 0 \\ x^2 & \text{if } x \leq -4 \end{cases}$$

Graph $g(x)$ and find its Domain and Range.

Each person turn in your own solutions.

You do need to understand ALL of these problems.

I will post answer keys on the class webpage.