

HW 18 Answer Key

$$1. \quad y' = \frac{1}{\ln x} \cdot \frac{1}{x} - e(\ln x)^{-2} \cdot \frac{1}{x} + e \cdot \frac{1}{x} + 0 + \frac{1}{e} \cdot \frac{1}{x} + 0 + (\ln x)e^x + e^x \cdot \frac{1}{x}$$

$$2. \quad f'(x) = \sec^2(\ln(1+x^2)) \cdot \frac{1}{1+x^2} \cdot (2x) + \frac{1}{1+\cos^2 x} \cdot 2\cos x (-\sin x) - 5(\ln(1+x^2))^2 \cdot \frac{1}{1+x^2} (2x)$$

$$3. \quad y' = \frac{4}{7} \left(\frac{1}{x^2+1} \right) (2x) + \sec^2 x - \frac{1}{2(1+\sqrt{x})} \cdot \frac{1}{2\sqrt{x}}$$

$$4. \quad \frac{dy}{dx} = 5^x \cdot (\ln 5)$$

$$5. \quad \frac{dy}{dx} = (\tan x)^x \left(\frac{x \sec^2 x}{\tan x} + \ln(\tan x) \right)$$

$$6. \quad f'(x) = e^{-\sin x} \cdot (-\cos x) - e(\sin(e^x))^{-2} \cdot \cos(e^x) e^x$$

$$7. \quad g''(x) = \frac{1}{2x\sqrt{\ln x}} + \frac{1}{2x}$$

$$8. \quad \text{Absolute Max Value } f(-1) = \textcircled{e}$$

$$9. \quad -\frac{9}{x} - \ln|x| + C$$

$$10. \quad \frac{8}{3}$$

$$11. \quad 1 - \ln|e-1|$$

$$12. \quad 2$$

$$13. \quad -\frac{1}{3} \ln |\cos(3x)| + C$$

$$14. \quad -\frac{1}{4} \ln\left(\frac{1}{3}\right) \quad \text{or} \quad \frac{1}{4} \ln\left(\frac{3}{7}\right)$$

$$15. \quad \frac{2}{3} + \ln 3$$

$$16. \quad \frac{1}{2} \ln 5 \quad \text{or} \quad \ln \sqrt{5}$$

$$17. \quad \frac{e^{-3x}}{-3} + 2x + \frac{e^{3x}}{3} + C$$

$$18. \quad f(x) = -\frac{1}{4(1-2e^{-2x})} - \frac{5}{4}$$

$$19. \quad y = 2x + 2$$

$$20. \quad y = -\frac{2}{9}x + \frac{2\ln 3}{9} + \frac{1}{9}$$